

Knowledge Organiser A Level Mathematics

Unit: Quantities and Units in Mechanics

Year: 12

Purpose of Unit:

- To introduce to the mechanics section of the A level

Key Learning/Knowledge:

- Quantities and units in mechanics

Key Skills:

- To know and use the language for mechanics modelling assumptions
- Units used in mechanics
- Converting to SI units

Key Vocabulary and meanings:

Model- a mathematical system which enables a problem to be solved

Light- has negligible mass

Static- not moving

Rigid- doesn't bend

Thin- has negligible thickness

Smooth- no friction between the surface and object

Rough- friction to be considered

Particle- dimensions are negligible so mass or object is at a point. Air resistance and rotational forces can be ignored

Rod- a long, thin, straight object

Lamina- a thin, two dimensional surface with mass distributed evenly across it's flat surface

Uniform body- mass is distributed evenly, so acts at the centre of mass

Light string- negligible mass and equal tension

Inextensible string- a string that does not stretch

Scalar- has magnitude only and is always positive. E.g. distance, speed, time, mass.

Vector- a quantity with magnitude and direction. E.g. velocity, acceleration

Links to prior knowledge/learning:

Converting between units of mass, volume and length.

Compound measures

Plotting and interpreting graphs

Cross Curricular link/ World Issues

Simplifying real world problems using the assumptions

Knowledge Organiser A Level Mathematics

Unit: Data Presentation and Interpretation

Year: 12

Purpose of Unit:

- To learn and embed the data presentation and interpretation content for the Statistics part of the A level.

Key Learning/Knowledge:

- To be able to calculate measures of location, mean, median and mode
- To be able to calculate measures of variation, standard deviation, variance, range and interpercentile range
- To be able to interpret and draw inferences from summary statistics
- Be able to clean data, including dealing with missing data, errors and outliers
- Interpret diagrams for single-variable data, including understanding that area in a histogram represents frequency
- Interpret scatter diagrams and regression lines for bivariate data, including recognition of scatter diagrams which include distinct sections of the population (calculations involving regression lines are excluded)
- Understand informal interpretation of correlation
- Understand that correlation does not imply causation
- Recognise and interpret possible outliers in data sets and statistical diagrams
- Select or critique data presentation techniques in the context of a statistical problem

Key Skills:

- Calculating averages
- Interpreting data
- Representing data
- Correlation

Links to prior knowledge/learning:

GCSE Data Handling

Cross Curricular link/ World Issues:

Large data set

Subjects such as psychology and the sciences also use advanced data handling skills.

Key Vocabulary and meanings:

Mean- The Arithmetic Mean is the average of the numbers: a calculated "central" value of a set of numbers

Median- The "middle" of a sorted list of numbers. This can be found from group data using **linear interpolation**.

Mode- The most common value of a set of data. A set of data can have more than one mode.

Variance- A measure of how spread out numbers are.

Standard deviation- also a measure of how spread out numbers are. This is the square root of the variance.

Skewness- When data has a "long tail" on one side or the other, so it is not symmetrical.

Interquartile range- Also a measure of how spread out the data is. This is the difference between the upper and lower quartiles.

Knowledge Organiser A Level Mathematics

Unit: Statistical Distributions

Year: 12

Purpose of Unit:

- To be able to find and use statistical probability distributions

Key Learning/Knowledge:

- Understand and use simple, discrete probability distributions including the Binomial Distribution
- Use the Binomial Distribution as a model
- Calculate probabilities using the Binomial Distribution

Key Vocabulary and meanings:

Binomial distribution- has two possible outcomes

Uniform distribution-all outcomes have the same probability of success

Discrete random variable- a set of possible values from an experiment

Cumulative- running total

Key Skills:

- Fractions, decimals and percentages
- Probability
- Quadratics
- Independent and mutually exclusive events

Links to prior knowledge/learning:

- Area under a curve
- GCSE Probability
- Using inequality symbols

Cross Curricular link/ World Issues

Probability experiments e.g. tossing a coin

Psychology

Sports

Knowledge Organiser A Level Mathematics

Unit: Constant acceleration

Year: 12

Purpose of Unit:

- To introduce constant acceleration

Key Learning/Knowledge:

- Distance-time and velocity time graphs
- SUVAT equations

Key Skills:

- Drawing and interpreting distance-time and velocity-time graphs
- Deciding which SUVAT equation is appropriate for the given problem
- Using SUVAT equations
- Vertical motion under gravity

Key Vocabulary and meanings:

Velocity- the rate of change of displacement

Acceleration- the rate of change of velocity

SUVAT equations-

$$v = u + at$$

$$v^2 = u^2 + 2as$$

$$s = ut + \frac{1}{2}at^2$$

$$s = vt - \frac{1}{2}at^2$$

$$s = \frac{1}{2}(u + v)t$$

s – displacement

u – initial velocity

v – final velocity

a – acceleration

t - time

Acceleration due to gravity- in maths we use 9.8m/s^2

Links to prior knowledge/learning:

Converting between SI and compound units (in previous unit)

Substitution into formulae

Changing the subject of a formula

Plotting and interpreting graphs in context

Cross Curricular link/ World Issues

This unit overlaps with the Physics A level.

Knowledge Organiser A Level Mathematics

Unit: Hypothesis Testing

Year: 12

Purpose of Unit:

- To perform hypothesis tests on the binomial distribution

Key Learning/Knowledge:

- Setting up hypothesis tests
- One tailed tests
- Two tailed tests
- Critical regions

Key Skills:

- Finding binomial probabilities
- Using inequality symbols

Key Vocabulary and meanings:

Null hypothesis- the hypothesis that there is no significant difference between the specified populations.

Alternate hypothesis- claims that there is a difference between the specified populations.

Significance level- a measure of the strength of the evidence that must be present in your sample before rejecting the null hypothesis.

Critical region- a set of values for the test statistic for which the null hypothesis is rejected

Links to prior knowledge/learning:

Previous unit on statistical distributions

Cross Curricular link/ World Issues

Hypothesis testing is used in real-life situations such as election polling
Biology, Psychology, Maths at degree level

Knowledge Organiser A Level Mathematics

Unit: Statistical Sampling

Year: 12

Purpose of Unit:

- To know and use statistical sampling methods and be introduced to the large data set

Key Learning/Knowledge:

- Sampling methods
- Large data set

Key Skills:

- To know and use 'population' and 'sample'
- Use samples to make inferences about a population
- To understand and use techniques including simple random, systematic, opportunity, quota and stratified sampling
- To critique sampling methods in context
- To familiarise with the large data set

Key Vocabulary and meanings:

Population- whole set of items that could be sampled

Census- observations taken from the entire population

Sample- observations taken from a subset of the population

Sampling unit- one individual observation set from the population

Sampling frame- a numbered (or named) list of individual sampling units

Strata- a subset of the population

Simple random sampling- every item has an equal chance of being chose e.g. random number generator

Quota sampling- non-random sample is taken to fill predetermined categories

Opportunity sampling- a non-random sample from available sampling units

Stratified sampling-random samples are taken proportionally from mutually exclusive groups

Systematic sampling-items are chosen at regular intervals from a sampling frame

Quantitative data- numerical values

Qualitative data- non-numerical values

Continuous data- variables that can take any value. Measured.

Discrete data- variables that can only take specific values. Counted.

Links to prior knowledge/learning:

GCSE data handling

Cross Curricular link/ World Issues

Psychology and sociology also use sampling methods

Knowledge Organiser A Level Mathematics

Unit: Forces and Newton's Laws

Year: 12

Purpose of Unit:

- To know and use Newton's laws of motion

Key Learning/Knowledge:

- Understand the concept of a force
- Understand and use Newton's first law
- Understand and use Newton's second law for motion in a straight line
- Understand and use Newton's third law
- Equilibrium of forces on a particle and motion in a straight line
- Application to problems involving smooth pulleys and connected particles

Key Skills:

- Draw force diagrams and calculate resultant forces
- Calculate resultant forces by adding vectors
- Form and solve equations using Newton's second law, $F = ma$
- Apply Newton's second law to vector forces and acceleration
- Solve problems involving connected particles

Key Vocabulary and meanings:

Force – a push or pull upon an object resulting from the object's interaction with another object

Mass - a measure of how much matter is in an object

Acceleration – the rate of change of velocity

Tension – the pulling force transmitted through a string, cable, or similar object

Equilibrium – the state of an object if all forces on it are balanced and therefore it's velocity does not change over time

Particle – object of negligible dimensions. The mass of the object is concentrated at a single point, air resistance and rotational forces can be ignored

Links to prior knowledge/learning:

- GCSE Calculating resultant vectors
- GCSE Trigonometry
- A-Level Modelling assumptions
- GCSE/A-Level Simultaneous Equations
- GCSE/A-Level physics Equations of motion

Cross Curricular link/ World Issues

- A-Level physics
- Design Technology
- Engineering

Knowledge Organiser A Level Mathematics

Unit: Probability

Year: 12

Purpose of Unit:

- To learn probability content for Year 12

Key Learning/Knowledge:

- Probability

Key Skills:

- Understand and use mutually exclusive and independent events when calculating probabilities
- Link to discrete and continuous distributions

Key Vocabulary and meanings:

Mutually exclusive-

Mutually exclusive events cannot happen at the same time

Independent-

Independent events do not affect each other.

$$P(A) \times P(B) = P(A \cap B)$$

Links to prior knowledge/learning:

GCSE Probability- frequency trees, tree diagrams, venn diagrams, sample space, exhaustive probability

Cross Curricular link/ World Issues

Probability has many real life applications such as the lottery, weather forecast, elections, card games etc.

Knowledge Organiser A Level Mathematics

Unit: Variable acceleration

Year: 12

Purpose of Unit:

- To learn how to solve problems with variable acceleration

Key Learning/Knowledge:

- To be able to use calculus (differentiation) in kinematics to model motion in a straight line for a particle moving with variable acceleration
- To understand that gradients of the relevant graphs link to rates of change
- To know how to find maximum and minimum velocities by considering zero gradients and understand how this links with the actual motion (i.e. acceleration = 0).
- To be able to use calculus (integration) in kinematics to model motion in a straight line for a particle moving under the action of a variable force
- To understand that the area under a graph is the integral, which leads to a physical quantity
- To know how to use initial conditions to calculate the constant of integration and refer back to the problem.

Key Vocabulary and meanings:

Displacement- how far from the starting point in a straight line. Usually measured in m.

Velocity- speed with direction. This can be obtained by differentiating the displacement or integrating the acceleration. Usually measured in m/s.

Acceleration- a measure of how fast the velocity changes. Usually measured in m/s^2 .

Key Skills:

- Differentiation
- Integration
- Displacement
- Velocity
- Acceleration

Links to prior knowledge/learning:

- Pure Maths Calculus
- Quadratic graphs
- Gradients

Cross Curricular link/ World Issues

- A Level Physics

Knowledge Organiser A Level Mathematics

Unit: Algebra and Functions

Year: 12

Purpose of Unit:

- To answer questions involving algebra and functions

Key Learning/Knowledge:

- Algebraic Expressions
- Quadratics
- Equations and Inequalities
- Graphs and Transformations

Key Skills:

- Laws of indices
- Manipulating surds
- Quadratic graphs
- Finding and using the discriminant
- Completing the square
- Solving quadratics
- Set notation
- Solving linear and quadratic inequalities
- Solving simultaneous equations algebraically and graphically
- Transformations of graphs

Key Vocabulary and meanings:

Integer- a whole number

Product- the answer when two or more values are multiplied together

Surd- a number that can't be simplified to remove a square root

Irrational- a real number that can NOT be made by dividing two integers e.g. π

Rational- a number that can be made by dividing two integers

Base- the number that gets multiplied when using an exponent

Quadratic- a function where the highest power is 2

Function- a special relationship where each input has a single output. Often written $f(x)$

Domain- the inputs of a function

Range- the outputs of a function

Discriminant- b^2-4ac is used to determine how many real roots a function has

Equation- a mathematical statement with an equals sign

Inequality- a mathematical statement comparing two values

Cubic- a function where the highest power is 3

Quartic- a function where the highest power is 4

Reciprocal function- a function where the highest power is negative

Asymptote- a line that a curve approaches as it heads to infinity or minus infinity

Links to prior knowledge/learning:

The majority of this unit has been covered at higher GCSE.

Cross Curricular link/ World Issues

- Using quadratics in modelling e.g. bridges
- Simultaneous equations in context
- Link to linear programming for optimisation problems

Knowledge Organiser A Level Mathematics

Unit: Further Algebra

Year: 13

Purpose of Unit:

- To cover the Further Algebra unit of the Maths A level

Key Learning/Knowledge:

- Factor theorem
- Algebraic division
- The Binomial expansion
- Algebraic proof

Key Skills:

- Manipulate polynomials algebraically, including expanding brackets and collecting like terms, factorisation and simple algebraic division; use of the factor theorem
- Understand and use the structure of mathematical proof, proceeding from given assumptions through a series of logical steps to a conclusion; use methods of proof, including: proof by deduction, proof by exhaustion, disproof by counter-example
- Understand and use the binomial expansion in the form $(a + bx)^n$

Key Vocabulary and meanings:

Binomial- an algebraic expression of the sum or difference of two terms

Coefficient-a number or symbol in front of a variable that represents a constant

Counter- example- an example that satisfies the statements conditions but does not support the statements conclusion

Conjecture-a mathematical statement that has not yet been rigorously proved.

Factor theorem- if $f(a)=0$, then $(x-a)$ is a factor.

Links to prior knowledge/learning:

GCSE knowledge- expanding and factorising brackets, substitution, proof

Cross Curricular link/ World Issues

Probability

Knowledge Organiser A Level Mathematics

Unit: Coordinate Geometry

Year: 12

Purpose of Unit:

- To cover A level content of coordinate geometry and prepare for future topics that will need this knowledge

Key Learning/Knowledge:

- Equation of a straight line
- Parallel and perpendicular lines
- Equation of a circle
- Multi- step problems
- Modelling

Key Skills:

- Understand and use proportional relationships and their graphs
- Understand and use the equation of a straight line
- Gradient conditions for two straight lines to be parallel or perpendicular
- To be able to find lengths and areas using equations of straight lines
- Be able to use straight line models in a variety of contexts
- Understand and use the coordinate geometry of a circle
- Complete the square to find the centre and radius of a circle
- Use circle theorems to solve more complex problems

Key Vocabulary and meanings:

Bisect- cut exactly in half

Parallel- parallel lines have the same gradient

Perpendicular- perpendicular lines meet at a right angle

Straight line equations-

$$Y=mx+c$$

$$ax+by+c=0$$

$$y-y_1=m(x-x_1)$$

Circle equation-

$$(x - a)^2 + (y - b)^2 = r^2$$

Where (a,b) is the centre and r is the radius.

Links to prior knowledge/learning:

GCSE skills- simultaneous equations, completing the square, equation of a line, parallel and perpendicular lines, trigonometry, Pythagoras' theorem, circle theorems

Cross Curricular link/ World Issues

Knowledge Organiser A Level Mathematics

Unit: Differentiation

Year: 12

Purpose of Unit:

- To be able to find and use the derivative of a function

Key Learning/Knowledge:

- Find the derivative, $f'(x)$ or $\frac{dy}{dx}$, of a function, including from first principles
- Use the derivative to solve problems involving gradient, tangents and normal
- Identify turning points and their nature
- Model real life situations with differentiation

Key Skills:

- To be able to find the derivative of a function from first principles
- To be able to differentiate x^n , quadratics and functions with 2 or more terms
- To be able to use the derivative to identify the gradient at a given point and the gradients of a tangent and normal
- To be able to identify whether a function is increasing or decreasing and to identify and interpret stationary points

Key Vocabulary and meanings:

Gradient – how steep a line is, or the rate of change of one variable with respect to another

Tangent - a straight line that touches a curve at a single point and therefore has the same gradient as the curve at that point

Normal – a straight line perpendicular to another line at a given point

Derivative – the rate at which an output changes with respect to an input

Differentiation – process used to find the derivative of a function

Links to prior knowledge/learning:

- GCSE Finding the gradient of a straight line
- GCSE Finding the gradient of a curve
- GCSE Sketching quadratics and other curved graphs
- GCSE Plotting and interpreting real-life graphs

Cross Curricular link/ World Issues

- A-Level physics
- Design Technology
- Engineering

Knowledge Organiser A Level Mathematics

Unit: Integration

Year: 12

Purpose of Unit:

- To be able to integrate a function

Key Learning/Knowledge:

- Find y , given $\frac{dy}{dx}$ for x^n
- Integrate polynomials
- Find $f(x)$, given $f'(x)$ and a point
- Evaluate definite integrals
- Find the area bounded by a curve and straight line

Key Skills:

- To be able to integrate x^n
- To be able to find indefinite integrals
- To be able to find a function given its derivative
- To be able to find the area under a curve

Key Vocabulary and meanings:

Integration – reverse process of differentiation, used to add slices to find a whole, e.g. to find the total area under a curve

Integral – the result of an integration.

Polynomial – expression made up of a combination of variables, constants and exponents

Derivative – the rate at which an output changes with respect to an input

Differentiation – process used to find the derivative of a function

Links to prior knowledge/learning:

- GCSE Finding the area of shapes formed by straight line on an axis
- GCSE Finding the area under a curve
- GCSE Sketching quadratics and other curved graphs
- GCSE Plotting and interpreting real-life graphs

Cross Curricular link/ World Issues

- A-Level physics
- Design Technology
- Engineering

Knowledge Organiser A Level Mathematics

Unit: Vectors

Year: 12

Purpose of Unit:

- To learn Year 12 vectors content and solve problems involving this

Key Learning/Knowledge:

- Use vectors in two dimensions
- Calculate the magnitude and direction of a vector and convert between component form and magnitude/direction form
- Add vectors diagrammatically and perform the algebraic operations of vector addition and multiplication by scalars, and understand their geometrical interpretations
- Understand and use position vectors; calculate the distance between two points represented by position vectors
- Use vectors to solve problems in pure mathematics and in context, (including forces)

Key Skills:

- Pythagoras' theorem
- Coordinate geometry
- Non right-angled trigonometry

Links to prior knowledge/learning:

GCSE vectors, surds, trigonometry

Cross Curricular link/ World Issues

A level Physics

A level Maths Mechanics

Engineering

There are many real-life applications, including any situation that involves force or velocity.

Key Vocabulary and meanings:

Vector- A vector has direction and magnitude

Scalar- A number on its own, used when dealing with vectors or matrices

Magnitude- The size of a vector

Direction- where a vector is pointing or heading

Position vector- a vector from a given point. At A level, this is usually the origin.

Knowledge Organiser A Level Mathematics

Unit: Exponentials and Logarithms

Year: 12

Purpose of Unit:

- To learn exponentials and logarithms content for year 1 of the course

Key Learning/Knowledge:

- To know what is meant by an exponential function
- To sketch graphs of exponential and logarithmic functions
- To solve problems with exponential modelling
- To know what is meant by a logarithm
- To simplify expressions using laws of logarithms
- To solve equations using logarithms
- To work with natural logarithms
- To use logarithms to estimate the values of constants in non-linear models

Key Skills:

- Laws of indices
- Substitution
- Plotting graphs
- Lines of best fit

Key Vocabulary and meanings:

Exponential-where a value increases or decreases in proportion to its current value

Logarithm- A logarithm answers the question "How many of this number do we multiply to get that number?"

Initial value- the starting value in context of the problem

Rate of change- the amount that the initial value is increasing or decreasing over time

Links to prior knowledge/learning:

Unit 1 Algebra and Functions

GCSE Algebra and Statistics

Cross Curricular link/ World Issues

A level Biology

Statistics part of the A level Maths course